- Congruent figures are figures with the same $\qquad$ and $\qquad$
- When 2 figures are congruent, you can move 1 so that it fits exactly on the other
- $\qquad$
$\qquad$ and $\qquad$ are all translations that result in congruent figures
- Can you think of a transformation from Unit 1 that would not result in a congruent figure?
- Congruent polygons have congruent $\qquad$ parts (matching sides and angles)
- When triangles are congruent, in proofs, we write $\qquad$ which stands for corresponding parts of congruent triangles are congruent
- When naming congruent polygons, always list corresponding vertices in the same order
- Write a congruence statement for the two triangles shown here:
$\qquad$
- Given: $\Delta \mathrm{WYS} \cong \Delta \mathrm{MKV}$. List the corresponding congruent parts without a picture.

$$
\circ \quad \angle W \cong
$$

$$
\circ \quad \angle S \cong
$$

$\qquad$

- $\angle Y \cong$ $\qquad$
- $\overline{W Y} \cong$ $\qquad$
- Write a congruence statement for the two triangles shown here:
$\qquad$ $\cong$ $\qquad$

Write a statement of congruence for each triangle below:
1)

2)


3)

- $\overline{\mathrm{YS}} \cong$ $\qquad$
- $\overline{S W} \cong$ $\qquad$
- Before we proved two triangles were congruent by showing that all six pairs of corresponding parts were congruent. It is possible to prove two triangles congruent using fewer parts.
(SSS) Congruence - If three sides of one triangle are congruent to three sides of a second triangle, then the triangles are congruent.
- $\qquad$ (SAS) Congruence - If two sides and the included angle of one triangle are congruent to two sides and the included angle of a second triangle, then the triangles are congruent.
- $\qquad$ (ASA) Congruence - If two angles and the included side of one triangle are congruent to two angles and the included side of another triangle, then the triangles are congruent.
- 

(AAS) Congruence - If two angles and the non-included side of one triangle are congruent to the corresponding two angles and side of a second triangle, then the two triangles are congruent.

State if the two triangles are congruent. If they are, state how you know. (SSS, SAS, ASA, and AAS).
1)

2)


3)

7)

4)

9)

10)

11)

12)



## Proving Triangles Congruent

- Reflexive Property of Triangle Congruence $\rightarrow \Delta \mathrm{ABC} \cong \triangle \mathrm{ABC}$
- Symmetric Property of Triangle Congruence $\rightarrow$ If $\triangle \mathrm{ABC} \cong \triangle E F G$, then $\triangle E F G \cong \triangle A B C$

Given the figure below, prove that $\triangle \mathrm{ACD} \cong \triangle \mathrm{CAB}$.


| Statement |  |
| :---: | :--- |
| 1. $\quad \mathrm{AB}=\mathrm{CD}, \overline{\mathrm{AB}} \\| \overline{\mathrm{CD}}$ |  |
| 2. $\angle \mathrm{BAC} \cong \angle \mathrm{DCA}$ |  |
| 3. $\mathrm{AC}=\mathrm{AC}$ |  |
| 4. $\quad \triangle \mathrm{ACD} \cong \triangle \mathrm{CAB}$ |  |

Given $\overline{\mathrm{AB}} \cong \overline{\mathrm{CD}}, \overline{\mathrm{AD}} \cong \overline{\mathrm{CB}}$, prove $\Delta \mathrm{ABD} \cong \Delta \mathrm{BCD}$.


| Statement |  |
| :---: | :--- |
| Reason |  |
| 1. $\overline{\mathrm{AB}} \cong \overline{\mathrm{CD}}$ |  |
| 2. $\overline{\mathrm{AD}} \cong \overline{\mathrm{CB}}$ |  |
| 3. $\overline{\mathrm{BD}} \cong \overline{\mathrm{BD}}$ |  |
| 4. $\Delta \mathrm{ABD} \cong \Delta \mathrm{CBD}$ |  |

Given the figure below, prove that $\triangle N P L \cong \triangle M P L$.


| Statement | Reason |
| :---: | :--- |
| 1. $\quad \mathrm{NP}=\mathrm{PM}, \overline{\mathrm{NP}} \perp \overline{\mathrm{PL}}$ |  |
| 2. $\angle \mathrm{MPL}$ is a right angle |  |
| $\angle \mathrm{NPL}$ is a right angle |  |
| 3. $\mathrm{PL}=\mathrm{PL}$ |  |
| 4. $\quad \triangle \mathrm{NPL} \cong \triangle \mathrm{MPL}$ |  |

I. Name the congruent triangles.

1. $\triangle O_{D} G D \cong \triangle$

2. $\triangle B O X \cong \Delta$ $\qquad$

II. For each pair of triangles, tell whether the triangles are congruent by a postulate. If they are write a similarity statement.
3. $\triangle \mathrm{ABC} \cong \Delta$

4. $\triangle \mathrm{ABC} \cong \Delta$ $\qquad$
$\qquad$

5. $\triangle \mathrm{ADC} \cong \Delta$ $\qquad$
$\qquad$

6. $\triangle \mathrm{ABE} \cong \Delta$ $\qquad$

7. $\triangle \mathrm{MNP} \cong \triangle$ $\qquad$


## Practice Proofs

For each pair of triangles, tell: (a) Are they congruent (b) Write the triangle congruency statement. (c) Give the postulate that makes them congruent. Then write a prove in the bale provided.
1.

a. $\qquad$
b. $\Delta$ $\qquad$ $\cong \Delta$ $\qquad$
c.

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

4. 


a.
b. $\Delta$ $\qquad$ $\cong \Delta$ $\qquad$
c.

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

7. 


a. $\qquad$
b. $\Delta$ $\qquad$ $\cong \Delta$
c. $\qquad$

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

2. 


a.
b. $\Delta \quad \simeq \Delta$
c.

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

5. 


a.
b. $\qquad$ $\cong \Delta$ $\qquad$
C. $\qquad$

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

8. 


a.
b. $\Delta$ $\qquad$ $\cong \Delta$ $\qquad$
c. $\qquad$

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

3. Given: $T$ is the midpoint of WR

a.
b. $\Delta \quad \sim \Delta$
c.

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

6. 


a.
b. $\Delta$
c.

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

9. 


a.
b. $\Delta$ $\qquad$ $\cong \Delta$
c. $\qquad$

| Statement | Reason |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |

